

1 Empirical Estimation of Daytime Net Radiation from Shortwave Radiation and

2 Ancillary Information

3 Bo Jiang¹, Yi Zhang², Shunlin Liang^{1, 2}, Georg Wohlfahrt³, Altaf Arain⁴, Alessandro

4 Cescatti⁵, Teodoro Georgiadis⁶, Kun Jia¹, Gerard Kiely⁷, Magnus Lund⁸, Leonardo

5 Montagnani⁹, Vincenzo Magliulo¹⁰, Penelope Serrano Ortiz¹¹, Walter Oechel¹²,

6 Francesco Primo Vaccari¹³, Yunjun Yao¹, Xiaotong Zhang¹

7 *1. State Key Laboratory of Remote Sensing Science, and School of Geography, Beijing Normal*
8 *University, Beijing 100875, China; 2. Department of Geographical Sciences, University of Maryland,*
9 *College Park, MD 20742, USA; 3. Institute of Ecology, University of Innsbruck, Innsbruck, Austria; 4.*
10 *School of Geography and Earth Sciences and McMaster Centre for Climate Change, McMaster*
11 *University, Hamilton, Ontario, Canada L8S4K1; 5. European Commission, Joint Research Center,*
12 *Institute for Environment and Sustainability, Ispra, Italy; 6. CNR-Institute of Biometeorology, via*
13 *Gobetti 101, 40129 Bologna, Italy; 7. Civil and Environmental Engineering, and Environmental*
14 *Research Institute, University College Cork, Ireland; 8. Arctic Research Centre, Department of*
15 *Bioscience, Aarhus University, Frederiksborgvej 399, DK-4000 Roskilde, Denmark; 9. Faculty of*
16 *Science and Technology, Free University of Bolzano, Piazza Università 5, 39100 Bolzano, Italy; 10.*
17 *CNR-ISAFOM, Institute for Mediterranean Agricultural and Forest Systems, National Research*
18 *Council, via Patacca 85, 80040 Ercolano (Napoli), Italy; 11. Dpto. Ecología, Facultad de Ciencias,*
19 *Universidad de Granada; 12. Global Change Research Group, San Diego State University, San Diego,*
20 *CA 92182, USA; 13. IBIMET-CNR Institute of Biometeorology National Research Council, via G.*
21 *Caproni 8, 50145 Firenze, Italy*

22 Corresponding author: Bo Jiang (bojiang@bnu.edu.cn)

23 **Abstract**

24 All-wave net surface radiation is greatly needed in various scientific research and
25 applications. Satellite data have been used to estimate incident shortwave radiation,
26 but hardly to estimate all-wave net radiation due to the inference of clouds on
27 longwave radiation. A practical solution is to estimate all-wave net radiation

28 empirically from shortwave radiation and other ancillary information. Since existing
29 models were developed using a limited number of ground observations, a
30 comprehensive evaluation of these models using a global network of representative
31 measurements is urgently required. In this study, we developed a new day-time net
32 radiation estimation model and evaluated it against seven commonly used existing
33 models using radiation measurements obtained from 326 sites around the world from
34 1991–2010. MERRA re-analysis products from which the meteorological data were
35 derived and remotely sensed products during the same period were also used. Model
36 evaluations were performed in both global mode (all data were used to fit the models)
37 and conditional mode (the data were divided into four subsets based on the surface
38 albedo and vegetation index, and the models were fitted separately). Besides, the
39 factors (i.e. albedo, air temperature, and NDVI) that may impact the estimation of
40 all-wave net radiation were also extensively explored. Based on these evaluations, the
41 fitting RMSE of the new developed model was approximately 40.0 Wm^{-2} in the global
42 mode and varied between 18.2 and 54.0 Wm^{-2} in the conditional mode. We found that
43 it is better to use net shortwave radiation (including surface albedo) than the incident
44 shortwave radiation nearly in all models. Overall, the new model performed better
45 than other existing linear models.

46 **Keywords:** Net radiation, Shortwave radiation, Empirical model, Remotely sensed
47 product

48 1. Introduction

49 All-wave net surface radiation (R_n) constitutes the available radiative energy at
50 the surface, and as such regulates most biological and physical processes, such as
51 evapotranspiration (Lu et al., 2014; Lu et al., 2013; Wang and Liang, 2008),
52 photosynthesis and turbulent and conductive heat fluxes. Thus, accurate estimates of
53 R_n are essential for understanding the land surface energy distribution, the formation
54 and transformation of air masses, snow melting calculations (Male and Granger, 1981),
55 modeling crop growth, and addressing water resource management (Bisht and Bras,
56 2011; Hwang et al., 2012). Estimation of R_n is necessary because it is a key input
57 for land surface process models, and are also used routinely to calculate
58 evapotranspiration (Monteith, 1965), which is a critical component of agricultural,
59 hydrological, and ecological research.

60

61 R_n is the difference between the incoming and outgoing shortwave and longwave
62 radiation fluxes at the surface. Mathematically described as:

$$\begin{aligned} R_n &= R_{ns} + R_{nl} \\ R_{ns} &= R_{si} - R_{so} = (1 - \alpha)R_{si} \\ R_{nl} &= R_{li} - R_{lo} \end{aligned} \quad (1)$$

64 Where R_{si} is the incoming shortwave radiation (Wm^{-2}), R_{so} is the reflected outgoing
65 shortwave radiation (Wm^{-2}), which is calculated by $R_{so} = \alpha * R_{si}$, α is the shortwave
66 broadband albedo (dimensionless), thus R_{ns} is the net shortwave radiation, R_{li} is the

67 incoming longwave radiation (Wm^{-2}), R_{lo} is the outgoing longwave radiation (Wm^{-2}),
68 and R_{nl} is the net longwave radiation (Wm^{-2}). R_n is normally positive during the
69 daytime because net shortwave radiation dominates, but negative during the nighttime
70 because net longwave radiation dominates (Allen et al., 1998).

71

72 If all four components of Eq. (1) are known, the calculation of R_n is
73 straightforward. Indeed, many radiation measurement towers measure these four
74 components of radiation, thereby allowing us to determine R_n at individual points.
75 Various satellite observations have been used to generate radiation products at
76 regional and global scales (Liang et al., 2010; Liang et al., 2013b; Tang and Li, 2008;
77 Tang et al., 2006; Wang and Liang, 2009b; Zhang et al., 2014). Satellite observations
78 from the visible to near-infrared spectrum have been used for estimating incident solar
79 radiation and surface albedo, and thermal-infrared data for estimating longwave
80 radiation. There are roughly two types of algorithms for estimating radiation(Liang et
81 al., 2010), one calculates radiative quantities from the derived satellite products of
82 all relevant atmospheric and surface variables (e.g., aerosol, cloud, atmospheric
83 temperature profile), and another estimates radiation directly from satellite observed
84 radiance using a regression equation established from extensive radiative transfer
85 simulations.

86

87 However, frequent cloud coverage implies that it is extremely difficult to estimate R_n

88 directly from satellite data, particularly longwave radiation component, because
89 clouds block the surface information from reaching the sensors. Since incident
90 shortwave radiation dominates day-time net radiation, methods have been developed
91 to estimate the incident shortwave radiation from satellite data (Liang et al., 2010).
92 Satellite data include information from both atmosphere and surface. From the
93 “clearest” observations (less atmospheric signals) during a temporal window, surface
94 reflectance/albedo can be retrieved, which can be assumed invariant during a short
95 period of time. As long as surface information is known, we can determine the
96 remaining atmospheric component that leads to estimation of incident shortwave
97 radiation (Liang et al., 2006). One of the challenges is the need for multiple
98 observations during a day for estimating day-time radiation but most polar-orbiting
99 satellite sensors, such as MODIS, observe the same surface only a couple of times
100 daily. One solution is to combine both polar-orbiting satellite data with geostationary
101 satellite(Zhang et al., 2014), for example, the Global Land Surface Satellite (GLASS)
102 radiation products at 5km spatial resolution and 3-hour temporal resolution(Liang et
103 al., 2013a; Liang et al., 2013c). Thus, an important research goal presently is to
104 develop robust methods for the empirical estimation of R_n from incident shortwave
105 radiation.

106

107 Although important information can be derived from sustained and uninterrupted
108 measurements of R_n over a surface, R_n measurements are only available from a small

109 number of representative radiometric observatories because expensive instruments
110 and constant maintenance are required (Monteith and Unsworth, 1990). To overcome
111 the lack of experimental observations, R_n needs therefore to be estimated from
112 empirical relationships based on physical considerations and meteorological data.
113 From a practical view point, it is important that R_n can be determined from
114 relationships that are not location-dependent so they are more universally applicable
115 and easy to use (Al-Riahi et al., 2003). Consequently, numerous attempts have been
116 made to calculate R_n based on different empirical methods. Two main types of
117 empirical methods can be classified according to previous studies. The first type of
118 methods estimates R_n from incoming shortwave radiation R_{si} and other meteorological
119 variables using simple linear regression (see Section 2.1.1). The second type of
120 methods estimates R_n by calculating the individual components in Eq.(1) separately,
121 where each component is estimated empirically or physically (Allen et al., 2011). The
122 first type of methods is used more widely, while the second one often generates
123 hybrid models with mixed empirical and physical sub-models.

124

125 Many of these empirical models were developed based on observational data from
126 specific locations. Thus, evaluating their performance in various environmental
127 conditions is a critical issue. Several studies have been conducted to evaluate the
128 performance of various empirical R_n estimation methods. Iziomon et al. (2000)
129 compared four types of regression models in three sites at different altitudes in the

130 southern Upper Rhine valley between Germany and Switzerland, and defined a model
131 as a “basic regression model” where R_n was only related to R_{si} . The limitations
132 associated with basic regression models were identified and improvements were
133 suggested such as incorporating a clearness index for characterizing the effects of
134 clouds on both shortwave and longwave radiation and air temperature for better
135 estimation of longwave radiation (see equations (4) and (6) below). Alados et al.
136 (2003) also compared the basic regression model with a model that was modified by
137 including albedo and seasonal information for a period of 38 months at a semi-arid
138 region site in Southeastern Spain. They concluded that seasonal information yielded
139 significant improvements for a semi-arid shrubland, but only slight improvements
140 were obtained by incorporating albedo information. Kjaersgaard et al. (2007) tested
141 six commonly used empirical models, including basic regression, multivariate
142 regression, and hybrid models coupled to physical Stefan-Boltzmann relationships, at
143 two independent temperate sites in Denmark for 32 and 7 years. Kjaersgaard et al.
144 (2009) focused mainly on comparisons of three net longwave radiation
145 parameterization models under two climate regimes in Denmark and Spain
146 respectively. Kjaersgaard et al. (2007) showed that various regression models that rely
147 on the local calibration of model coefficients should be derived from a time series that
148 comprises at least 5 years of data, and they also showed that physically-based models
149 are more suitable. They concluded that the performance of these models is generally
150 best in the summertime and worst in the wintertime. Better performance in the

151 summertime and worse performance in the wintertime for various radiation
152 parameterization schemes, both the physical and empirical, are due to the higher
153 signal-to-noise ratio (STNR) for higher magnitudes of radiation in the summertime
154 but lower STNR for lower magnitudes of radiation in the wintertime. Similarly,
155 Sentelhas and Gillespie(2008) evaluated four types of models to estimate the hourly
156 R_n at a grass site in mid-latitudes in Canada for a 58-day period during the growing
157 season in 2003. These models were based on different combinations of R_{si} ,
158 meteorological variables (air temperature and relative humidity), and cloud cover
159 information. The results showed that these models performed well and they were
160 generally able to obtain similar hourly R_n values as measured, but they performed
161 better in clear sky conditions rather than overcast conditions, and the incorporation of
162 cloud information did not seem to significantly improve these estimates of R_n . The
163 reason for better performances of these models in clear sky conditions is exactly the
164 same as in the summertime because of the higher STNR of the radiation
165 measurements.

166

167 Most previous studies have evaluated empirical R_n estimation methods in different
168 environmental conditions as described above, but they still have several limitations.
169 The number of R_n validation sites used in early works was in fact typically less than
170 five, which means that the land cover and climatic conditions encompassed were
171 limited, so that the conclusions of these studies are not suitable to be adopted

172 universally. Also, since long-term time series of radiation measurements are not easy
173 to collect, most studies focused on a short-term period. Several studies have suggested
174 that at least 5-year observations are needed for fitting empirical models (Kjaersgaard
175 et al., 2007; Wang and Liang, 2009a). This may be one of the reasons why the
176 performance of the same model varied greatly among studies. Another important
177 limitation of these empirical approaches is that they do not accommodate terrain
178 effects on incoming solar radiation. This simplification could result in significant
179 errors over mountainous areas where aspect, slope, and elevation can greatly
180 determine the globe incoming solar radiation and consequently net radiation for
181 applications associated with ET estimation, ecosystem and climate modeling (Gao et
182 al., 2008; Long et al., 2010; Wu et al., 2006). Finally, new empirical models that use
183 shortwave radiation developed recently have not been evaluated and compared with
184 other models.

185

186 The objective of this study is to identify the most robust empirical models for
187 estimating daytime (defined as the time period between sunrise and sunset) R_n from
188 incident and/or net shortwave radiation and other meteorological variables that are
189 suitable to be used at global scale. The strategy to achieve this objective is to collect
190 the most comprehensive and representative ground measurements data sets across the
191 world to test all available empirical models. In this study, observed radiation data
192 were obtained from 326 sites, and were collected around the world since the 1990s

193 from 12 observing networks. Based on these evaluations, we propose a new empirical
194 model for estimating the daytime R_n .

195

196 The remainder of this paper is organized as follows. The different models are
197 introduced in Section 2. Section 2 also describes the site information, remotely sensed
198 and re-analysis data, and the data processing procedure. The results of the analyses
199 and discussions are presented in Section 3. A Summary is given in Sections 4.

200 **2. Methodology and data**

201 **2.1 Methodology**

202 2.1.1 Overview of the empirical models

203 We present seven types of empirical models and their common feature is that the R_n is
204 estimated linearly from the incoming shortwave radiation.

205

206 Model 1 (*mod1*) is the simplest:

$$207 \quad R_n = a_1 R_{si} + b_1 \quad (2)$$

208 where a_1 and b_1 are coefficients. The main advantage of *mod1* is its simplicity since
209 its only requirement is the incoming shortwave radiation. However, *mod1* does not
210 correct for the net longwave radiation or for the seasonal changes in surface albedo
211 (Kjaersgaard et al., 2007 1213).

212

213 Model 2 (*mod2*) is very similar to *mod1* but it uses net shortwave radiation instead.

214 The implicit inclusion of albedo was first introduced by Kaminsky and

215 Dubayah(1997):

216
$$R_n = a_2 R_{ns} + b_2 = a_2 R_{si} (1 - \alpha) + b_2 \quad (3)$$

217 where a_2 and b_2 are coefficients. The authors concluded that the use of net shortwave

218 radiation can make the model almost independent of the cloud cover, time of day, or

219 day of year.

220

221 To take into account the impacts of clouds, Iziomon et al. (2000) found that the

222 inclusion of a clearness index ($CI = \frac{R_{si}}{R_{se}}$) can improve the daytime R_n estimation:

223
$$R_n = a_3 R_{si} + b_3 CI + c_3 \quad (4)$$

224 where a_3 , b_3 , and c_3 are coefficients, CI is the clearness index (dimensionless), and R_{se}

225 is the extra-terrestrial irradiance, which is calculated as follows(Irmak et al., 2003):

226
$$R_{se} = \frac{1440 G_{sc} d_r}{\pi} [\omega_s \sin(\phi) \sin(\delta) + \cos(\phi) \cos(\delta) \sin(\omega_s)]$$
$$d_r = 1 + 0.033 \cos\left(\frac{2\pi DOY}{365}\right)$$
$$\delta = 0.409 \sin\left(\frac{2\pi DOY}{365} - 1.39\right)$$
$$\omega_s = \arccos[-\tan(\phi) \tan(\delta)] \quad (5)$$

227 where G_{sc} is the solar constant ($0.0820 \text{ MJm}^{-2} \cdot \text{min}^{-1}$), d_r is the inverse relative

228 distance from the Earth to the Sun, ω_s is the sunset hour angle (*rad*), ϕ is the latitude

229 (rad), δ is the solar declination (rad), and DOY is the day of the year. This model is
230 defined as *mod3* in this study.

231

232 Iziomon et al. (2000) also found that surface air temperature affects the estimation of
233 longwave radiation and eventually net radiation, and this model is defined as *mod4*:

$$234 \quad R_n = a_4 R_{si} (1 - \alpha) + b_4 \sigma T_{a,K}^4 + c_4 \quad (6)$$

235 where $T_{a,K}$ is the absolute air temperature, σ =Stefan-Boltzmann constant
236 ($5.67 \times 10^{-8} WK^{-4} m^{-2}$), and a_4 , b_4 , and c_4 are coefficients. Surface air temperature

237 determines downward longwave radiation of the atmosphere, and also is a proxy of

238 surface skin temperature that largely determines surface upwelling longwave radiation,

239 The authors found out that *mod4* performed better monthly than hourly.

240

241 Irmak et al. (2003) also linked R_n to a set of meteorological variables. However,

242 Kjaersgaard et al. (2007) showed that some variables (i.e., the daily maximum and

243 minimum air temperatures) are inter-correlated, which may cause multicollinearity

244 and make the prediction model less stable. Therefore, the regression model proposed

245 by Irmak et al.(2003) was modified by Kjaersgaard et al.(2007), and this model is

246 defined as *mod5* as follows:

$$247 \quad R_n = a_5 R_{si} + b_5 T_{a,^{\circ}C} + c_5 d_r + d_5 \quad (7)$$

248 Where $T_{a,^{\circ}C}$ is the mean air temperature ($^{\circ}C$), d_r is the inverse relative Earth-Sun

249 distance defined in Eq. (5), and a_5 , b_5 , c_5 , and d_5 are coefficients. Kjaersgaard et

250 al.(2007) concluded that *mod5* tended to overestimate R_n slightly in some seasons but
 251 it still performed better than the original model proposed by (Irmak et al., 2003).

252

253 Holtslag and Van Ulden(1983) proposed a relationship between the shortwave net
 254 radiation, surface air temperature and cloud cover:

$$255 \quad R_n = \frac{R_{si}(1-\alpha) + D_1 T_{a,K}^6 - \sigma T_{a,K}^4 + D_2 N}{1 + D_3} \quad (8)$$

256 where $D_1 = 5.31 \times 10^{-13} \text{ Wm}^{-2} \cdot \text{K}^{-6}$ is an empirical constant suggested by
 257 Swinbank(1963), N is the total cloud cover fraction, $T_{a,K}$ is mean daily absolute air
 258 temperature (K), D_2 and D_3 are also empirical constants, and D_3 denotes the heating
 259 coefficient for the surface. The authors treated the term $D_1 T_{a,K}^6$ as the theoretical
 260 incoming longwave radiation and $\sigma T_{a,K}^4$ as the theoretical outgoing longwave
 261 radiation. Thus, $R_{si}(1-\alpha) + D_1 T_{a,K}^6 - \sigma T_{a,K}^4$ represents the theoretical net radiation,
 262 while all the other terms are used to correct the theoretical net radiation to the actual
 263 net radiation. Cloud data were not easy to collect, so we used $N = 1 - CI$ instead in the
 264 present study. D_2 and D_3 have been derived by Al-Riahi et al.(2003) using locally
 265 collected data. Therefore, we modified the original model as follows and defined it as
 266 *mod6*:

$$267 \quad R_n = a_6 [R_{si}(1-\alpha) + D_1 T_{a,K}^6 - \sigma T_{a,K}^4] + b_6 CI + c_7 \quad (9)$$

268 where a_6 , b_6 , and c_7 are coefficients. Al-Riahi et al.(2003) validated the original model
 269 (Eq. (8)) in an area of Baghdad that was covered by grass and found that the model
 270 performance was best under clear sky conditions ($R^2 > 0.99$ in summer).

271

272 Although *mod6* incorporates the influence of clouds, the impact of the land surface is
273 not considered. Learning from the study of Wang and Liang(2009a) (see also equation
274 (11)), the normalized difference vegetation index (NDVI) could be a good indicator to
275 represent the land surface in R_n estimation. Therefore, we improved *mod6* by
276 incorporating the remotely sensed NDVI and relative humidity ($RH_{\%}$) after multiple
277 trial experiments, and we denote this model as “*modnew*”:

$$278 \quad Rn = a_{new} [R_{si} (1 - \alpha) + D_1 T_{a,K}^6 - \sigma T_{a,K}^4] + b_{new} CI \quad (10)$$
$$\quad \quad \quad + c_{new} NDVI + d_{new} RH_{\%} + e_{new}$$

279 where a_{new} , b_{new} , c_{new} , d_{new} , and e_{new} are coefficients, and the other variables are the
280 same as those used in *mod6*.

281

282 Wang and Liang (2009a) developed a multivariate linear regression model based on
283 solar shortwave radiation and conventional meteorological observations and satellite
284 retrievals (NDVI and albedo), as follows:

$$285 \quad R_n = R_{si} (1 - \alpha) (a + b T_{min, \circ C} + c DT_{a, \circ C} + d NDVI + e RH_{\%}) \quad (11)$$

286 where $T_{min, \circ C}$ is the daily minimum air temperature and $DT_{a, \circ C}$ is the daily diurnal air
287 temperature range. It was found that this model could readily generate a large bias, so
288 a constant term was added in this study. To ensure consistency, this model (*mod7*) is
289 expressed as follows:

$$290 \quad R_n = R_{si} (1 - \alpha) (a_7 + b_7 T_{min, \circ C} + c_7 DT_{a, \circ C} + d_7 NDVI + e_7 RH_{\%}) + f_7 \quad (12)$$

291 where a_7 , b_7 , c_7 , d_7 , e_7 , and f_7 are coefficients. To incorporate the contribution of

292 elevation, $T_{min, c}$ is corrected for sea level by decreasing the temperature by 6.5°C for
293 each 1-km increase in elevation (Wang and Liang, 2009a). This model is the first to
294 consider surface elevation. After validation using measurements at 24 sites worldwide,
295 it was demonstrated that the original model (Eq. (11)) provided good estimates of the
296 daytime R_n for all sky conditions with bias varying from 27.8 to 9.7 W m^{-2} (63% in
297 relative value) for different sites, and RMSE from 12.8 to 21 W m^{-2} (from 15% to 19%
298 in relative value) for different sites, and an average of 16.9 W m^{-2} (16% relative) for
299 all sites.

300

301 Many studies have discussed whether the estimates of R_n can be improved by
302 incorporating surface albedo in the empirical models, but no consensus has been
303 reached. To better understand the effect of albedo, the models with R_{ns} or R_{si}
304 (*mod3–mod7*) were modified by replacement with R_{si} , or R_{ns} (by setting albedo equal
305 to 0 or not) respectively. Because *mod2* is the modified *mod1*, therefore, seven
306 original linear regression models (*mod1–mod7*) and five modified models
307 (*mod3'–mod7'*) were evaluated in the present study.

308 2.1.2 Cross-validation procedure for model evaluation

309 R_n estimation methods studied here were evaluated based on a leave-one-out
310 cross-validation procedure. The observations from one site were used for validation
311 and the observations from all other sites we used for model fitting. The procedure was
312 repeated and the statistics of the validation results were compiled. Three measures

313 were used to characterize the model performance: R^2 , root mean squared error
314 (RMSE), and bias. In general, all three measures were examined to evaluate the
315 performance of various models, but RMSE values were given larger weights.

316 **2.2Data**

317 The data used in this study comprised the in-situ radiation measurements, remote
318 sensing products, and meteorological reanalysis data. The remote sensing products
319 and reanalysis data were used to map net radiation on a global scale. After multiple
320 trial experiments, no significant differences in estimated R_n with the eight models by
321 using daily or daytime meteorological data was found. Therefore, after pre-processing
322 with strict quality control, all of these data were aggregated to a daily scale except
323 radiation measurements which were aggregated to a daytime scale. Further details of
324 these data are given below.

325 2.2.1In-situration observations

326 (1)Measurement networks

327 The observed net radiation data were collected from 326 sites in 12 global
328 measurement networks, as shown in Fig.1. These sites are distributed across the globe
329 and represent different climatic and ecosystem conditions, which range from the
330 Arctic to the Antarctic. Some two thirds of these sites may be ascribed to the La
331 Thuile dataset of the FLUXNET network. Table 1 provides more information on each
332 network.

333

334 The land cover types at these sites, as defined by the International
335 Geosphere-Biosphere Programme (IGBP), included evergreen broadleaf forest,
336 evergreen needle-leaf forest, deciduous broadleaf forest, deciduous needle-leaf forest,
337 mixed forest, cropland, grassland, savanna, ice, barren or sparse vegetation, wetland
338 and shrubland (Table 2). The elevations of these sites ranged from -0.7m to 5063m
339 above sea level. This comprehensive representation of land cover types, widespread
340 spatial distribution, and different elevations ensured that the global applicability of the
341 models was assessed.

342 Note that some of these locations where observations of net radiation were made
343 did not have associated meteorological measurements like air temperature, wind, etc.,
344 so that model reanalysis was needed for these variables.

345 (2) Daytime radiation pre-processing

346 The radiation measurements came from different observation networks, so various
347 pre-processing procedures were required. It is noteworthy that the La Thuile dataset is
348 temporally continuous because its missing data have been filled using a time-filling
349 methods (Falge et al., 2001). However, other datasets have not been filled in this study.
350 The observation times for each site have been transformed into the solar time for
351 consistency, and then the radiation observations (R_n and R_{si}) were aggregated into the
352 daytime mean values. The “daytime” in this study is defined as the time period

353 between sunrise and sunset, so the sunrise and sunset times for each site should be
354 determined firstly according to Doggett et al.(1978). After that, the daytime
355 radiation values were calculated by averaging all the observations between sunrise
356 and sunset for each site. To ensure quality control, the daytime values were only
357 calculated if at least one observation was available in each single hour during daytime
358 hours. Finally, all of the daytime values were checked manually, and any
359 unreasonable values were removed.

360

361 Note that the methods proposed by Doggett et al. (1978) for estimating the sunrise
362 and sunset times does not account for the effect of terrain on solar radiation, which
363 may limit its applications over complex terrain.

364 2.2.2 Satellite products

365 Land surface changes can be characterized by the long time series NDVI and
366 surface albedo, so two satellite products (*NDVI* and surface albedo) were used in this
367 study to explore the effects of land surface characteristics on the surface net radiation
368 estimates. To match the long term period of the radiation measurements, the
369 bi-weekly 8-km NDVI products from 1982-2010 derived from the Advanced High
370 Resolution Radiometer (AVHRR) data on the National Oceanic and Atmospheric
371 Administration (NOAA) polar-orbiting satellite by the NASA Global Inventory
372 Monitoring and Modeling Studies (GIMMS) (Tucker et al., 2005) and the 8-day
373 0.05° spatial resolution albedo products from 1982-2010 extracted from the Global

374 Land Surface Satellite (GLASS) datasets were used in this study. The AVHRR
375 GIMMS NDVI product has been used widely (Jiang and Liang, 2013; Zhang et al.,
376 2013), and the GLASS albedo product has been demonstrated to be more accurate
377 than other products(Liang et al., 2013a; Liang et al., 2013c; Liu et al., 2013a; Qu et al.,
378 2014). The NDVI and albedo time series data were extracted for each site.

379 For all these models discussed in Section 2.111, ground measured incident
380 shortwave radiation data (R_{si}) and the corresponding satellite albedo product (α)
381 for calculating R_{ns} were used in this study. However, satellite products will need to be
382 used when applying these models to map net radiation at the global scale, which is
383 one of the objectives in the phase-II GLASS project. GLASS shortwave radiation
384 product (R_{si}) has 5km and 3h resolutions currently only from 2008-2010 (Liang et al.,
385 2013a; Liang et al., 2013c; Zhang et al., 2014), but it is being extended to cover
386 multiple years.

387 2.2.3 Reanalysis data

388 Meteorological reanalysis data were used for global mapping in the present study
389 because of the limited coverage of the field meteorological observation networks. We
390 used NASA Modern Era Retrospective-Analysis for Research and Applications
391 (MERRA) data (Rienecker et al., 2011). Multiple meteorological variables, including
392 maximum air temperature (T_{max} , °C), minimum air temperature (T_{min} , °C), mean air
393 temperature (T_a , °C), diurnal temperature range (DT , °C), wind speed (W , m/s), and
394 surface air pressure (PS , pa), were first extracted for each site from 1982–2010, and

395 the hourly MERRA data were then aggregated to obtain daily values. The relative
 396 humidity ($RH\%$) cannot be extracted from MERRA directly, so it was calculated from
 397 other MERRA quantities (<http://www.cactus2000.de/uk/unit/masshum.shtml>):

$$398 \quad RH\% = \frac{PS_{pa} / ((m_{dry} qv_{kg/kg} + m_{h_2o} - m_{h_2o} qv_{kg/kg}) / (qv_{kg/kg} m_{dry}))}{a_0 + T_{a,^{\circ}C} (a_1 + T_{a,^{\circ}C} (a_2 + T_{a,^{\circ}C} (a_3 + T_{a,^{\circ}C} (a_4 + T_{a,^{\circ}C} (a_5 + T_{a,^{\circ}C} a_6 / 1000))))))} \quad (13)$$

399 where PS_{pa} is the surface air pressure, and $qv_{kg/kg}$ is the specific humidity from
 400 MERRA. m_{dry} and m_{h_2o} are the molar mass of dry air and water, and they were
 401 defined as 28.9644 g/mol and 18.01534 g/mol respectively. The denominator is used
 402 for vapor pressure of water calculation (Lowe and Ficke, 1974). The other constants
 403 are defined as: $a_0 = 6.107799961$, $a_1 = 0.443651$, $a_2 = 1.4289 \times 10^{-2}$, $a_3 = 2.65 \times$
 404 10^{-4} , $a_4 = 3.03 \times 10^{-6}$, $a_5 = 2.03 \times 10^{-8}$, and $a_6 = 6.1368 \times 10^{-8}$.

405

406 3. Results and discussion

407 After pre-processing, 414,540 observations were used from 326 sites during
 408 1992–2010. The models were fitted with these observations in two cases. In case 1, the
 409 models were fitted using all the observations, i.e., *global models*. In case 2, the
 410 observations were divided into several subsets based on their surface characteristics
 411 (see Section 3.1.2) and the models obtained are referred to as *conditional models*.

412 3.1 Model evaluation results

413 3.1.1 Global model

414 The performances of all the empirical models based on the cross-validations are
415 shown in Table 3. The results show that including the surface albedo generally
416 produced better fitting results. For example, the regression statistics of *mod3* was
417 improved, where R^2 increased from 0.823 to 0.888, RMSE decreased from 52.895 to
418 42.005Wm^{-2} , and bias changed from -0.069 to 0.019Wm^{-2} when R_{si} was replaced with
419 R_{ns} . Similar improvements were obtained with *mod5*. However, the fitting accuracy
420 declined when R_{ns} was replaced with R_{si} in *mod4*, *mod6*, *mod7* and *modnew*. Among
421 all the models, *modnew* and *mod7* had the best performance, followed by *mod4* and
422 *mod6*. The modified models *mod3'* and *mod5'* performed as well as *mod4* and *mod6*.

423 In Fig. 2 three measures of the fitting statistics (R^2 , RMSE, and bias) are
424 compared, where only the best for each model was selected (*mod1*, *mod2*, *mod3'*,
425 *mod4*, *mod5'*, *mod6*, *mod7*, and *modnew*). Note that all of the models selected
426 included R_{ns} . *Mod7* and *modnew* yielded higher R^2 values, lower RMSE, and almost
427 zero bias. The other models delivered similar R_n fitting performance.

428 The coefficients of the eight global models (*mod1*–*modnew*) using all of the
429 observations from 326 sites are shown in Table4. All of the dependent variables were
430 significant ($p < 0.05$). Only the best model in each case is shown in this table.

431 To better understand the differences in our results compared with previous studies,

432 the original coefficients of some published models are shown in Table5, as well as
433 their fitting statistics using all of the measurements in the present study. Although
434 many studies employed calibrated model coefficients, some coefficients could not be
435 used for comparison in the present study due to the different time scales employed
436 (daily/monthly), thus only five models were selected. As earlier, only the best variants
437 for each model are shown here, where *mod1*, *mod2*, *mod4*, and the revised *mod3*
438 (*mod3'*—containing R_{ns}) and *mod7* (containing the bias term) were compared with the
439 original published models. Note that the coefficients for Linacre (1992) and Iziomon
440 et al. (2000) in Table 5 are the median coefficients from 19 sites and three sites in
441 their studies respectively. In general, the coefficients of *mod1* and *mod2* were similar
442 in different studies, but the model bias became smaller when more sites were used for
443 fitting. For *mod3*, the coefficients differed considerably because R_{ns} was used in our
444 study and it is obvious that the model fitting accuracy was improved significantly by
445 using *mod3'*, with the RMSE of 41.81 and the bias of -0.003 Wm^{-2} . The coefficients
446 were also different for *mod4* and the model-data mismatch was worse than that
447 obtained using the original model. For *mod7*, the coefficients were different due to
448 the addition of the bias term, although the bias decreased near zero using the new
449 model. Therefore, the comparative results indicate the importance of using
450 comprehensive measurements when fitting empirical models.

451 3.1.2 Conditional model

452 In the global model, the models had fixed coefficients for all land surfaces. Most

453 previous studies focused on a small region or on a few sites, thus they were unable to
454 discuss the effects of land surface on the net radiation. By contrast, the extensive
455 observations used in the present study were collected globally (Fig.1), so it was
456 possible for us to explore the conditional mode, i.e., fitting models in specific
457 conditions.

458 After multiple trial experiments, we found that the relationships between R_{si} and
459 R_n differed with various combinations of surface $NDVI$ and albedo. The models tested
460 in our study were all based on the relationship between R_n and shortwave radiation, so
461 we divided the entire dataset into the subsets based on the $NDVI$ and albedo according
462 to the different relationships between R_{si} and R_n , as shown in Fig.3. Fig. 3a and 3c
463 show the scatter plots for R_{si} and R_n with different $NDVI$ values and their
464 corresponding albedo histograms (Fig. 3b and 3d). An $NDVI$ threshold of 0.2 was
465 selected to identify vegetated surfaces that have similar albedo values. When
466 $NDVI < 0.2$ (no vegetation, Fig.3a), the non-vegetated surfaces (Fig.3b) were
467 categorized into three classes: $albedo \leq 0.25$, $0.25 < albedo < 0.7$, and $albedo \geq 0.7$, and
468 Fig.4 shows that the relationships between R_{si} and R_n differed considerably among the
469 three classes. However, the relation between R_{si} and R_n (Fig.3c) was similar with
470 vegetated surfaces ($NDVI \geq 0.2$). Thus, four categories were identified, as shown in
471 Table 6.

472 Table 6 shows the four classification criteria and the corresponding numbers of
473 observations for the conditional models. For simplicity, we denote the four categories

474 as S1 ($NDVI < 0.2$ and $albedo \leq 0.25$), S2 ($NDVI < 0.2$ and $0.25 < albedo < 0.7$), S3
475 ($NDVI < 0.2$ and $albedo \geq 0.7$), and S4 ($NDVI \geq 0.2$). These four categories
476 corresponded to some of the major land cover types found on the Earth. For
477 example, S1 can represent wetland, S2 represents desert or barren land with sparse
478 vegetation, S3 represents snow/ice, and S4 represents the remaining vegetation
479 surface types. Furthermore, the seasonal information can also be represented by these
480 categories. In the following, the performances of the eight net radiation estimation
481 models are discussed with the four individual categories.

482 Similar to the global model evaluation, the performance of these models and those
483 modified by replacing R_{si} (R_{sn}) with R_{sn} (R_{si}) were also compared based on these four
484 categories. To eliminate the effects of NDVI values in S1–S3, the *NDVI* values were
485 set to 0. For simplicity, only the best fitting result was selected for each model for
486 comparison, and the final model selection results are shown in Table 7, which shows
487 that the fitting accuracy was improved by incorporating albedo for most of the
488 categories and empirical models, except *mod7* and *modnew* for S1.

489 Fig. 5 shows the comparative results for all models with the different categories.
490 For class S1, *modnew*' yielded the best performance, followed by *mod2* and *mod3*'
491 with similar performances levels, and *mod7*' had the highest bias, although R^2 (0.775)
492 and RMSE (55.415 Wm^{-2}) were good. For class S2, *mod2*, *mod3*', *mod6*, and *modnew*
493 yielded similar regression accuracy, although *mod3*' was the best, whereas *mod7* only

494 performed better than *mod1*, which had the poorest performance. However, the
495 overall fitting accuracies for S2 were not as good as those for S1 and S4, which
496 indicates that the use of incoming shortwave radiation for -estimating R_n is more
497 suitable for non-vegetated surfaces with low albedo or other ordinary land surface
498 types. Compared with the other categories, S3 was very different because there was
499 nonlinear relationship between R_{si} and R_n (Fig. 4). Nearly all of these models had
500 similar performance. The average R^2 was only around 0.1, but the RMSE values were
501 very small compared to those in other cases and the biases were nearly zero. Keep in
502 mind that net radiation of snow/ice surfaces is relatively small because of high albedo.
503 The comparison showed that *mod2* yielded the best performance for S3. *Modnew* was
504 the model with the best performance for S4.

505 Overall, several conclusions can be made based on these results: (1) the new
506 model *modnew* that was developed in the present study had the best performance and
507 it was very stable with the four categories; (2) unlike other models, the fitting results
508 could not be improved by introducing albedo in *mod7* and *modnew* for class S1 (see
509 Table 7); (3) *mod1* only used R_{si} and it yielded the worst performance in general.

510 In summary, all empirical net radiation fitting models that included shortwave
511 radiation could be used for net radiation estimation in most situations because their
512 fitting accuracy was acceptable despite some differences from each other. In particular,
513 net radiation is difficult to estimate over a surface that has no vegetation or sparse
514 vegetation and high albedo, thus the physically-based or longwave radiation

515 parameterization models or non-linear models should be considered in this case.

516 **3.2 Discussions**

517 Previous studies of net radiation estimation models have assessed the impacts of
518 surface albedo, air temperature, and surface elevation, but their conclusions are
519 inconsistent and not comprehensive. In the present study, we tested these models
520 simply by studying the relationships between the measured and simulated R_n , as well
521 as related factors (e.g., surface albedo, NDVI, air temperature), for each model in
522 every category (S1, S2, S3, S4 and global). Due to unavailability of cloud data, the
523 clearness index (CI) was used instead. We observed that the relationships between the
524 fitting errors and other factors were very similar for all models in each category,
525 where the daily air mean/minimum temperature, wind speed and CI were the most
526 sensitive factors during net radiation estimation. We consider *modnew* as an example.

527 Fig. 6a-e show the relationships between the net radiation fitting errors and the
528 daily air mean temperature. In general, the fitting errors were greater with higher air
529 temperature, except for class S1. Higher air temperature may correspond to a hotter
530 season (summer), near noon local time, or low latitude, which generally have larger
531 incident shortwave radiation and therefore net radiation. Thus, it is reasonable to have
532 larger absolutely errors. Besides, higher air temperature also leads to larger longwave
533 radiation.

534 For wind speed (Fig. 6f-j), the fitting errors were greater with smaller wind speeds,
535 except for class S1. Weaker wind may indicate warmer air and larger incident

536 shortwave radiation and longwave radiation. Their relative errors may not display the
537 similar trends.

538 The influence of cloud was very similar for all categories. Fig. 6k-o show that the
539 fitting errors were smaller when the sky was overcast, which is consistent with the
540 previous findings (Alados et al., 2003; Kaminsky and Dubayah, 1997). It may be also
541 explained by the reduced absolute magnitude of incident solar radiation under cloudy
542 conditions.

543 We also studied the effects of elevation on net radiation estimation. The air
544 temperature is usually scaled by elevation in the models, but we found that scaling the
545 air temperature by elevation did not make much difference.

546 Therefore, the effects of air temperature and cloud may consider to be
547 incorporated into the estimation models in future research because satellite remote
548 sensing is capable of producing accurate products of air temperature and cloud
549 coverage. Although wind cannot be accurately retrieved over land surfaces from
550 satellite data, if our speculations discussed above are right, wind effects can be
551 addressed if models incorporate the information of air temperature and cloud
552 coverage.

553 **4. Summary**

554 Due to the inadequate spatial representation of field measurements, satellite
555 remote sensing provides a practical method for mapping net radiation spatially and

556 temporally at different scales. A practical solution is to estimate the net radiation
557 empirically based on the incoming shortwave radiation or shortwave net radiation,
558 which can be estimated accurately from satellite observations. To develop a robust
559 empirical model, we collected as many comprehensive ground measurements as
560 possible and evaluated the most commonly used empirical models.

561

562 We evaluated seven daytime net radiation estimation empirical models using
563 observations obtained from 326 independent sites during 1992–2010. These sites were
564 distributed worldwide and they represented the major land cover types on the Earth,
565 as well as seasonal information. The leave-one-out cross-validation method was used
566 to derive calibration coefficients and for validation. The performances of these models
567 were evaluated using the whole dataset (*global model*) or four subsets based on the
568 surface albedo and *NDVI* values (*conditional model*). The effects of albedo, elevation,
569 and some meteorological factors were investigated in the present study.

570

571 Based on extensive evaluations and analyses of existing models, we developed a
572 new model that performed better than the existing models in both the global and
573 conditional models. In the global model, the RMSE of this new model was
574 approximately 40.0 Wm^{-2} . In the conditional mode, the new model could reduce the
575 RMSEs to 53.92, 50.99, 18.23, and 39.01 Wm^{-2} for S1–S4, respectively, which were
576 better results than those obtained using most of the other linear empirical models

577 considered in this study.

578

579 Noting that these models evaluated in this study are linear based on the linear
580 relationships between all-wave net radiation and incident surface shortwave radiation
581 or surface shortwave net radiation, but the possible non-linear relations have not been
582 considered here but presented elsewhere (Jiang et al. 2014). The global distribution of
583 the observations used in this study is largely biased toward the boreal regions and
584 western countries, and few urban sites were included. And also the terrain slope and
585 orientation of these radiation measurements have not been taken into account in this
586 study. Besides, the remotely sensed and reanalysis data used have coarser spatial
587 resolution, and may not be the best to match the site radiation observations. All these
588 aspects need to be addressed in the future.

589 **Acknowledgements**

590 This study was funded partly by the National High-Technology Research and
591 Development Program of China under Grant 2013AA122800, the Fundamental
592 Research Funds for the Central Universities (ID: 2013NT28), and the Natural Science
593 Foundation of China (No. 41401381 and No. 41331173). This work used eddy
594 covariance data acquired by the FLUXNET community and in particular by the
595 following networks: AmeriFlux (U.S. Department of Energy, Biological and
596 Environmental Research, Terrestrial Carbon Program (DE-FG02-04ER63917)),

597 AfriFlux, AsiaFlux, CarboAfrica, CarboEuropeIP, CarboItaly, CarboMont, ChinaFlux,
598 Fluxnet-Canada (supported by CFCAS, NSERC, BIOCAP, Environment Canada, and
599 NRCan), GreenGrass, KoFlux, LBA, NECC, OzFlux, TCOS-Siberia, USCCC. We
600 acknowledge the financial support to the eddy covariance data harmonization
601 provided by CarboEuropeIP, FAO-GTOS-TCO, Ileaps, Max Planck Institute for
602 Biogeochemistry, National Science Foundation, University of Tuscia, Université
603 Laval, Environment Canada and US Department of Energy and the datasets
604 development and technical support from Berkeley Water Center, Lawrence Berkeley
605 National Laboratory, Microsoft Research Science, Oak Ridge National Laboratory,
606 University of California – Berkeley and the University of Virginia. We also would like
607 to thank other radiation measurements providers (their names are listed in Table 1). In
608 particular, we thank Dr. Yan Li and Dr. Ran Li from the Xinjiang Institute of Ecology
609 and Geography, CAS, and Dr. Jean Christophe Calvet from CNRM-GAME for
610 sharing their data. We would like to thank two anonymous reviewers for their
611 valuable comments and suggestions that have greatly improved the presentation of
612 this paper.

613 **References**

- 614 Al-Riahi, M., Al-Jumaily, K. and Kamies, I., 2003. Measurements of net radiation and
615 its components in semi-arid climate of Baghdad. *Energy Conversion and*
616 *Management*, 44(4): 509-525.
- 617 Alados, I., Foyo-Moreno, I., Olmo, F.J. and Alados-Arboledas, L., 2003. Relationship
618 between net radiation and solar radiation for semi-arid shrub-land. *Agricultural*
619 *and Forest Meteorology*, 116(3-4): 221-227.

620 Allen, R. et al., 2011. Satellite-based ET estimation in agriculture using SEBAL and
621 METRIC. *Hydrological Processes*, 25(26): 4011-4027.

622 Allen, R.G., Pereira, L.S., Raes, D. and Smith, M., 1998. Crop
623 evapotranspiration-Guidelines for computing crop water requirements-FAO
624 Irrigation and drainage paper 56. FAO, Rome, 300: 6541.

625 Augustine, J.A., DeLuisi, J.J. and Long, C.N., 2000. SURFRAD—A National Surface
626 Radiation Budget Network for Atmospheric Research. *Bulletin of the
627 American Meteorological Society*, 81(10): 2341-2357.

628 Augustine, J.A., Hodges, G.B., Cornwall, C.R., Michalsky, J.J. and Medina, C.I.,
629 2005. An Update on SURFRAD—The GCOS Surface Radiation Budget
630 Network for the Continental United States. *Journal of Atmospheric and
631 Oceanic Technology*, 22(10): 1460-1472.

632 Bisht, G. and Bras, R.L., 2011. Estimation of Net Radiation From the Moderate
633 Resolution Imaging Spectroradiometer Over the Continental United States.
634 *IEEE transactions on geoscience and remote sensing*, 49(6): 2448-2462.

635 de Rosnay, P. et al., 2006. SMOSREX: A long term field campaign experiment for soil
636 moisture and land surface processes remote sensing. *Remote Sensing of
637 Environment*, 102(3-4): 377-389.

638 Doggett, L., Kaplan, G. and Seidelmann, P., 1978. Almanac for computers, 1978.
639 Nautical Almanac Office, United States Naval Observatory, Washington DC,
640 USA, pp. B5.

641 Falge, E. et al., 2001. Gap filling strategies for defensible annual sums of net
642 ecosystem exchange. *Agricultural and Forest Meteorology*, 107(1): 43-69.

643 Gao, Y., Long, D. and Li, Z.-L., 2008. Estimation of daily actual evapotranspiration
644 from remotely sensed data under complex terrain over the upper Chao river
645 basin in North China. *International Journal of Remote Sensing*, 29(11):
646 3295-3315.

647 Holtslag, A. and Van Ulden, A., 1983. A simple scheme for daytime estimates of the
648 surface fluxes from routine weather data. *Journal of Climate and Applied
649 Meteorology*, 22(4): 517-529.

650 Hwang, K., Choi, M., Lee, S. and Seo, J.-W., 2012. Estimation of instantaneous and
651 daily net radiation from MODIS data under clear sky conditions: a case study
652 in East Asia. *Irrigation Science*: 1-12.

653 Irmak, S., Irmak, A., Jones, J., Howell, T., Jacobs, J., Allen, R., and Hoogenboom, G.,
654 2003. Predicting Daily Net Radiation Using Minimum Climatological Data.
655 *Journal of Irrigation and Drainage Engineering*, 129(4): 256-269.

656 Iziomon, M.G., Mayer, H. and Matzarakis, A., 2000. Empirical Models for Estimating
657 Net Radiative Flux: A Case Study for Three Mid-Latitude Sites with
658 Orographic Variability. *Astrophysics and Space Science*, 273(1): 313-330.

659 Jia, Z.Z., Liu, S.M., Xu, Z.W., Chen, Y.J. and Zhu, M.J., 2012. Validation of remotely
660 sensed evapotranspiration over the Hai River Basin, China. *Journal of
661 Geophysical Research-Atmospheres*, 117.

662 Jiang, B., Zhang, Y., Liang, S.L., Zhang X.T., and Xiao, Z.Q., 2014. Surface Daytime
663 Net Radiation Estimation Using Artificial Neural Networks. *Remote Sensing*,
664 6: 11031-11050.

665 Jiang, B. and Liang, S.L., 2013. Improved vegetation greenness increases summer
666 atmospheric water vapor over Northern China. *Journal of Geophysical
667 Research: Atmospheres*, 118: 1-11.

668 Kaminsky, K.Z. and Dubayah, R., 1997. Estimation of surface net radiation in the
669 boreal forest and northern prairie from shortwave flux measurements. *Journal
670 of Geophysical Research-Atmospheres*, 102(D24): 29707-29716.

671 Kjaersgaard, J., Cuenca, R., Plauborg, F. and Hansen, S., 2007. Long-term
672 comparisons of net radiation calculation schemes. *Boundary-Layer
673 Meteorology*, 123(3): 417-431.

674 Kjaersgaard, J.H. et al., 2009. Comparison of the performance of net radiation
675 calculation models. *Theoretical and Applied Climatology*, 98(1-2): 57-66.

676 Liang, S., Zhao, X., Liu, S.H., Yuan, W.P., Cheng, X., Xiao, Z.Q., Zhang, X.T., Liu,
677 Q., Cheng, J., Tang, H.R., Qu, Y.H., Bo, Y.C., Qu, Y., Ren, H.Z., Yu, K., and
678 Townshend, J., 2013a. A long-term Global LAnd Surface Satellite (GLASS)
679 data-set for environmental studies. *International Journal of Digital Earth*,
680 6(sup1): 5-33.

681 Liang, S., Zheng, T., Liu, R., Fang, H., Tsav, S.C., and Running, S., 2006. Mapping
682 incident Photosynthetically Active Radiation (PAR) from MODIS Data.
683 *Journal of Geophysical Research - Atmospheres*, 111, Art. No. D15208.

684 Liang, S.L., Wang, K.C., Zhang, X.T. and Wild, M., 2010. Review on Estimation of
685 Land Surface Radiation and Energy Budgets From Ground Measurement,
686 Remote Sensing and Model Simulations. *Selected Topics in Applied Earth
687 Observations and Remote Sensing*, IEEE Journal of, 3(3): 225-240.

688 Liang, S.L., Zhang, X.T., He, T., Cheng, J. and Wang, D.D., 2013b. Remote sensing
689 of earth surface radiation budget. In: G.P. Petropoulos (Editor), *Remote
690 Sensing of Land Surface Turbulent Fluxes and Soil Surface moisture Content:
691 State of the Art*. CRC Press, pp. 125-165.

692 Liang, S.L., Zhang, X.T., Xiao, Z.Q., Cheng, J., Liu, Q., and Zhao, X., 2013c. Global
693 LAnd Surface Satellite (GLASS) products: Algorithms, Validation and
694 Analysis. Springer.

695 Linacre, E., 1992. *Climate data and resources: a reference and guide*.

696 Liu, Q., Wang, L.Z., Qu, Y., Liu, N.F., Liu, S.H., Tang, H.R., and Liang, S.L., 2013a.
697 Preliminary evaluation of the long-term GLASS albedo product. *International
698 Journal of Digital Earth*, 6: 69-95.

699 Liu, S.M., Xu, Z.W., Wang, W.Z., Jia, Z.Z., Zhu, M.J., Bai, J., and Wang, J.M., 2011.
700 A comparison of eddy-covariance and large aperture scintillometer
701 measurements with respect to the energy balance closure problem. *Hydrology
702 and Earth System Sciences*, 15(4): 1291-1306.

703 Liu, S.M., Xu, Z.W., Zhu, Z.L., Jia, Z.Z. and Zhu, M.J., 2013b. Measurements of

704 evapotranspiration from eddy-covariance systems and large aperture
705 scintillometers in the Hai River Basin, China. *Journal of Hydrology*, 487(0):
706 24-38.

707 Long, D., Gao, Y. and Singh, V.P., 2010. Estimation of daily average net radiation
708 from MODIS data and DEM over the Baiyangdian watershed in North China
709 for clear sky days. *Journal of Hydrology*, 388(3-4): 217-233.

710 Lowe, P.R. and Ficke, J.M., 1974. The computation of saturation vapor pressure,
711 DTIC Document.

712 Lu, J., Tang, R.L., Tang, H.J., Li, Z.L., Zhou, G.Q., Shao, K., Bi, Y.Y., and Labeled, J.,
713 2014. Daily Evaporative Fraction Parameterization Scheme Driven by
714 Day-Night Differences in Surface Parameters: Improvement and Validation.
715 *Remote Sensing*, 6(5): 4369-4390.

716 Lu, J., Tang, R.L., Tang, H.J. and Li, Z.L., 2013. Derivation of Daily Evaporative
717 Fraction Based on Temporal Variations in Surface Temperature, Air
718 Temperature, and Net Radiation. *Remote Sensing*, 5(10): 5369-5396.

719 Male, D. and Granger, R., 1981. Snow surface energy exchange. *Water Resources*
720 *Research*, 17(3): 609-627.

721 Monteith, J.L., 1965. Evaporation and environment, *Symposia of the Society for*
722 *Experimental Biology* pp. 205-224.

723 Monteith, J.L. and Unsworth, M.H., 1990. *Principles of Environmental Physics*.
724 Edward Arnold, London, UK, pp. 291.

725 Ohmura, A., Gilgen, H., Hegner, H., Müller, G., Wild, M., Dutton, E.G., Forgan, B.,
726 Fröhlich, C., Philipona, R., Heimo, A., König-Langlo, G., McArthur, B.,
727 Pinker, R., Whitlock, C.H., and Dehne, K., 1998. Baseline Surface Radiation
728 Network (BSRN/WCRP): New Precision Radiometry for Climate Research.
729 *Bulletin of the American Meteorological Society*, 79(10): 2115-2136.

730 Qu, Y., Liu, Q., Liang, S.L., Wang, L.Z., Liu, N.F., and Liu, S.H., 2014. Improved
731 mapping daily land-surface broadband albedo from MODIS data. *IEEE*
732 *Geoscience and Remote Sensing Letters*, 52: 907-919.

733 Rienecker, M.M., Suarez M.J., Gelaro R., Todling R., Bacmeister J., Liu E.,
734 Bosilovich M.G., Schubert S.D., Takacs L., Kim G.K., Bloom S., Chen J.Y.,
735 Collins D., Conaty A., Da Silva A., Gu W., Joiner J., Koster R.D., Lucchesi R.,
736 Molod A., Owens T., Pawson S., Pegion P., Redder C.R., Reichle R.,
737 Robertson F.R., Ruddick A.G., Sienkiewicz M., and Wollen J., 2011. MERRA:
738 NASA's Modern-Era Retrospective Analysis for Research and Applications.
739 *Journal of Climate*, 24(14): 3624-3648.

740 Sentelhas, P.C. and Gillespie, T.J., 2008. Estimating hourly net radiation for leaf
741 wetness duration using the Penman-Monteith equation. *Theoretical and*
742 *Applied Climatology*, 91(1): 205-215.

743 Steffen, K., Box, J. and Abdalati, W., 1996. Greenland climate network: GC-Net. US
744 Army Cold Regions Reattach and Engineering (CRREL), CRREL Special

745 Report: 98-103.

746 Swinbank, W.C., 1963. Longwave radiation from clear skies. *QJR Meteorol Soc*, 89:
747 339-348.

748 Tang, B. and Li, Z.-L., 2008. Estimation of instantaneous net surface longwave
749 radiation from MODIS cloud-free data. *Remote Sensing of Environment*,
750 112(9): 3482-3492.

751 Tang, B., Li, Z.-L. and Zhang, R., 2006. A direct method for estimating net surface
752 shortwave radiation from MODIS data. *Remote Sensing of Environment*,
753 103(1): 115-126.

754 Tucker, C.J., Pinzon J.E., Brown M.E., Slayback D.A., Pak E.W., Mahoney R.,
755 Vermote E.F., and El Saleous N., 2005. An extended AVHRR 8-km NDVI
756 dataset compatible with MODIS and SPOT vegetation NDVI data.
757 *International Journal of Remote Sensing*, 26(20): 4485-4498.

758 Wang, K. and Liang, S., 2009a. Estimation of Daytime Net Radiation from Shortwave
759 Radiation Measurements and Meteorological Observations. *Journal of Applied
760 Meteorology and Climatology*, 48(3): 634-643.

761 Wang, K.C. and Liang, S.L., 2008. An improved method for estimating global
762 evapotranspiration based on satellite determination of surface net radiation,
763 vegetation index, temperature, and soil moisture. *Journal of
764 Hydrometeorology*, 9(4): 712-727.

765 Wang, W.H. and Liang, S.L., 2009b. Estimation of high-spatial resolution clear-sky
766 longwave downward and net radiation over land surfaces from MODIS data.
767 *Remote Sensing of Environment*, 113(4): 745-754.

768 Wu, W., Hall, C.A.S., Scatena, F.N. and Quackenbush, L.J., 2006. Spatial modelling
769 of evapotranspiration in the luquillo experimental forest of puertorico using
770 remotely-sensed data. *J. Hydrol.*, 328: 733-752.

771 Xu, Z.W., Liu S.M., Li X., Shi S.J, Wang J.M., Zhu Z.L., Xu T.R., Wang W.Z., and
772 Ma M.G., 2013. Intercomparison of surface energy flux measurement systems
773 used during the HiWATER-MUSOEXE. *Journal of Geophysical
774 Research-Atmospheres*, 118(23): 13140-13157.

775 Zhang, G., Zhang, Y., Dong, J. and Xiao, X., 2013. Green-up dates in the Tibetan
776 Plateau have continuously advanced from 1982 to 2011. *Proceedings of the
777 National Academy of Sciences of the United States of America*, 110(11):
778 4309-4314.

779 Zhang, X., Liang, S., Zhou, G.S., Wu, H. and Zhao, X., 2014. Generating Global
780 LAnd Surface Satellite incident shortwave radiation and photosynthetically
781 active radiation products from multiple satellite data. *Remote Sensing of
782 Environment*, 152: 318-332.

783

784

785 **Tables**

786 Table 1 Information related to the 12 observation networks

| Network/ Program | No. of sites | Time Period | Instrument | URL |
|---|-------------------------|------------------------|----------------------------------|--|
| Global Fluxnet (La Thuile dataset) | 207 | 1991-2008 | Kipp&ZonenCNR-1, etc. | http://www.fluxdata.org/ |
| AsiaFlux | 19 | 1999-2008 | Kipp&Zonen CNR-1 | http://www.asiaflux.net/ |
| ARM | 22 | 2002-2013 | Kipp&Zonen CNR-1 | https://www.arm.gov/ |
| BSRN | 6 | 1992-2012 | Eppley, PIR/Kipp&Zonen CG4 | http://www.bsrn.awi.de/ |
| SURFRAD | 7 | 1995-2012 | Eppley, PIR | http://www.esrl.noaa.gov/gmd/gr ad/surfrad/ |
| GAME/AA N | 10 | 1997-2003 | EKO MS0202F | http://aan.suiri.tsukuba.ac.jp/aan. html |
| BOREAS | 5 | 1993-1996 | Kipp&Zonen CM-5 | http://daac.ornl.gov/BOREAS/bh s/BOREAS_Home.html |
| GC-Net | 13 | 1995-2012 | Li Cor Photodiode & REBS Q* 7 | http://cires.colorado.edu/science/ groups/steffen/gcnet/ |
| CEOP-GE WEX | 37 | 2002-2009 | Eppley, PIR/Kipp&Zonen CG4 | http://www.eol.ucar.edu/projects/ ceop/ |
| CEOP | 10 | 2007-2009 | | |
| SMOSREX | 1 | 2005-2010 | Kipp&Zonen CNR-1 | http://www.cesbio.ups-tlse.fr/us/s mos/smos_lewis.html |
| CERN | 1 | 2007 | | http://www.cerndata.ac.cn/ |

787 ARM: Atmospheric Radiation Measurement, BSRN: Baseline Surface Radiation Network(Ohmura et al., 1998),
788 SURFRAD: Surface Radiation Network(Augustine et al., 2000; Augustine et al., 2005), BOREAS: Boreal
789 Ecosystem-Atmosphere Study, GC-Net: Greenland Climate Network(Steffen et al., 1996), CEOP-GEWEX:
790 Coordinated Enhanced Observing Period, CEOP: Coordinated Enhanced Observation Network of China (Jia et al.,
791 2012; Liu et al., 2011; Liu et al., 2013b; Xu et al., 2013), SMOSREX: Surface Monitoring Of Soil Reservoir
792 Experiment(de Rosnay et al., 2006), CERN: Chinese Ecosystem Research Network.

793

794

795

Table 2 Number of sites for each IGBP land cover type

| IGBP Land Cover Types | No. of sites |
|--------------------------------------|---------------------|
| Barren& Sparse vegetation | 6 |
| Cropland | 50 |
| Deciduous Broadleaf Forest | 35 |
| Deciduous Needleleaf Forest | 6 |
| Evergreen Broadleaf Forest | 17 |
| Evergreen Needleleaf Forest | 68 |
| Grassland | 70 |
| Ice | 17 |
| Mixed Forest | 14 |
| Savanna | 7 |
| Shrubland | 18 |
| Wetland | 18 |
| Total | 326 |

796

797

798

799

800

801

802

803

804

805

806

807

808

809 Table 3 Comparative fitting statistics for seven daytime net radiation estimation models. The
 810 coefficients a and b are the slope and intercept of the linear regression relationship between estimated
 811 and measured R_n .

| | a | b ($W m^{-2}$) | R^2 | RMSE ($W m^{-2}$) | bias ($W m^{-2}$) | | a | b ($W m^{-2}$) | R^2 | RMSE ($W m^{-2}$) | bias ($W m^{-2}$) |
|---------------|--------|-----------------------|-------|------------------------|------------------------|----------------|--------|-----------------------|-------|------------------------|------------------------|
| <i>mod1</i> | 0.9991 | 0.167 | 0.767 | 60.634 | -0.0003 | | | | | | |
| <i>mod2*</i> | 0.9996 | 0.059 | 0.879 | 43.658 | -0.016 | | | | | | |
| <i>mod3</i> | 0.9992 | 0.083 | 0.823 | 52.895 | -0.069 | <i>mod3**</i> | 0.9990 | 0.207 | 0.888 | 42.005 | 0.019 |
| <i>mod4*</i> | 0.9992 | 0.135 | 0.886 | 42.385 | 0.018 | <i>mod4'</i> | 0.9989 | 0.098 | 0.827 | 52.361 | 0.1003 |
| <i>mod5</i> | 0.9990 | 0.048 | 0.828 | 52.114 | 0.143 | <i>mod5**</i> | 0.9994 | 0.088 | 0.887 | 42.209 | -0.028 |
| <i>mod6*</i> | 0.9991 | 0.163 | 0.890 | 41.641 | 0.002 | <i>mod6'</i> | 0.9991 | 0.095 | 0.826 | 52.474 | -0.077 |
| <i>mod7*</i> | 0.9986 | 0.209 | 0.899 | 39.882 | -0.045 | <i>mod7'</i> | 0.9984 | 0.250 | 0.867 | 45.901 | -0.045 |
| <i>modnew</i> | 0.9987 | 0.183 | 0.899 | 40.025 | -0.047 | <i>modnew'</i> | 0.9992 | 0.044 | 0.859 | 47.276 | -0.098 |

812 ' denotes a modified model, and * denotes models that included R_{ns} .

813
 814
 815
 816
 817
 818
 819
 820
 821
 822
 823
 824
 825

826

827 Table 4 Coefficients for the best eight global models

| Model | Coefficients | | | | | |
|-----------------|--------------|-----------|-----------|-----------|-----------|----------|
| <i>mod1</i> | a_1 | b_1 | | | | |
| | 0.654 | -20.317 | | | | |
| <i>mod2</i> * | a_2 | b_2 | | | | |
| | 0.781 | -13.596 | | | | |
| <i>mod3</i> '* | a_3 | b_3 | c_3 | | | |
| | 0.867 | -81.483 | 6.310 | | | |
| <i>mod4</i> * | a_4 | b_4 | c_4 | | | |
| | 0.724 | 0.211 | -77.253 | | | |
| <i>mod5</i> '* | a_5 | b_5 | c_5 | d_5 | | |
| | 0.721 | 0.777 | -301.420 | 296.842 | | |
| <i>mod6</i> * | a_6 | b_6 | c_6 | | | |
| | 0.863 | -90.491 | 87.219 | | | |
| <i>mod7</i> * | a_7 | b_7 | c_7 | d_7 | e_7 | f_7 |
| | 0.5515 | 0.0027 | 0.0015 | 0.1321 | 0.1652 | -10.7575 |
| <i>modnew</i> * | a_{new} | b_{new} | c_{new} | d_{new} | e_{new} | |
| | 0.862 | -65.435 | 24.564 | 54.351 | 20.966 | |

828 ' denotes a modified model, and * denotes models that included R_{ns} .

829

830

831

832

833

834

836 Table 5 Comparisons of the coefficients and performance using *mod1*, *mod2*, *mod3*, *mod4*, and *mod7* in
 837 the present study and the original published reports.

| | Coefficients | | | Model comparison | | |
|----------------------------------|-----------------------|-----------------------|-------|------------------|-----------------------------|--------------------------------|
| | | | | R ² | RMSE (Wm ⁻²) | bias (Wm ⁻²) |
| <i>mod1</i> | <i>a</i> ₁ | <i>b</i> ₁ | 0.767 | 60.425 | -0.0097 | |
| | 0.654 | -20.317 | | | | |
| Linacre (1992) | 0.63 | -23 | 0.769 | 60.425 | -10.118 | |
| <i>Iziomon et al.</i> (2000) | 0.63 | -25.7 | 0.769 | 60.425 | -12.818 | |
| <i>mod2</i> | <i>a</i> ₂ | <i>b</i> ₂ | 0.880 | 43.511 | 0.001 | |
| | 0.781 | -13.596 | | | | |
| <i>Iziomon et al.</i> (2000) | 0.80 | -24.5 | 0.880 | 43.511 | -6.104 | |
| <i>mod3'</i> | <i>a</i> ₃ | <i>b</i> ₃ | 0.889 | 41.810 | -0.003 | |
| | 0.867 | -81.483 | | | | <i>c</i> ₃ 6.310 |
| <i>Iziomon et al.</i> (2000)* | 0.77 | -147.5 | 0.817 | 53.829 | -24.575 | |
| <i>mod4</i> | <i>a</i> ₄ | <i>b</i> ₄ | 0.888 | 42.170 | -0.008 | |
| | | <i>c</i> ₄ | | | | |

| | | | | | | | | | |
|------------------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|-----------------------|--------|--------|--------|
| | 0.724 | 0.211 | -77.253 | | | | | | |
| <i>Iziomon et al.(2000)</i> | 0.82 | 0.028 | 38.4 | | 0.882 | 43.200 | 72.230 | | |
| <i>mod7</i> | <i>a</i> ₇ | <i>b</i> ₇ | <i>c</i> ₇ | <i>d</i> ₇ | <i>e</i> ₇ | <i>f</i> ₇ | 0.902 | 39.356 | -0.049 |
| | 0.5515 | 0.0027 | 0.0015 | 0.1321 | 0.1652 | -10.7575 | | | |
| <i>Wang and Liang(2009a)</i> | 0.5129 | 0.0025 | 0.0000 | 0.1401 | 0.2604 | | 0.899 | 39.883 | 13.251 |

838 * denotes the models that included R_{si} , where the others included R_{ns} .

839

840 Table 6 Four classification categories based on the combination of NDVI and albedo, with their
841 corresponding numbers of observations.

| Class | Classification criteria | No. of Observations |
|-------|---------------------------------|---------------------|
| S1 | NDVI<0.2 and albedo \leq 0.25 | 19111 |
| S2 | NDVI<0.2 and 0.25<albedo<0.7 | 17909 |
| S3 | NDVI<0.2 and albedo \geq 0.7 | 20229 |
| S4 | NDVI \geq 0.2 | 357291 |

842

843

844

845

846

847 Table 7 Final models selected for comparison for each category.

| | Selected models |
|----|--|
| S1 | <i>mod1, mod2*, mod3'*, mod4*, mod5'*, mod6*, mod7'_{ndvi=0}, modnew'_{ndvi=0}</i> |
| S2 | <i>mod1, mod2*, mod3'*, mod4*, mod5'*, mod6*, mod7*_{ndvi=0}, modnew*_{ndvi=0}</i> |
| S3 | <i>mod1, mod2*, mod3'*, mod4*, mod5'*, mod6*, mod7*_{ndvi=0}, modnew*_{ndvi=0}</i> |
| S4 | <i>mod1, mod2*, mod3'*, mod4*, mod5'*, mod6*, mod7*, modnew*</i> |

848 ' denotes a modified model, and * denotes the models that included R_{ns} .

849 Figure Caption

850 Figure 1 Distribution of 326 observation sites in 12 measurement networks.

851

852

853 Figure 2 Comparisons of the fitting statistics for the eight selected models (*mod1*,
 854 *mod2*, *mod3'*, *mod4*, *mod5'*, *mod6*, *mod7*, and *modnew*) using three measures: (a) R^2 ,
 855 (b) RMSE (Wm^{-2}), (c) bias (Wm^{-2}).

856

857

858 Figure 3 Scatter plots for R_n and R_{si} (a, c), and their corresponding histograms of
 859 albedo (b, d) when $NDVI < 0.2$ and $NDVI \geq 0.2$.

860

861

862 Figure 4 The scatter plot for R_n and R_{si} when classified by albedo whenever
 863 $NDVI < 0.2$.

864

865

866 Figure 5 Comparison of the fitting accuracies (R^2 , RMSE, bias) for eight selected
867 models with four categories: (a)-(c) S1, (d)-(f) S2, (g)-(i) S3, and (j)-(l) S4.

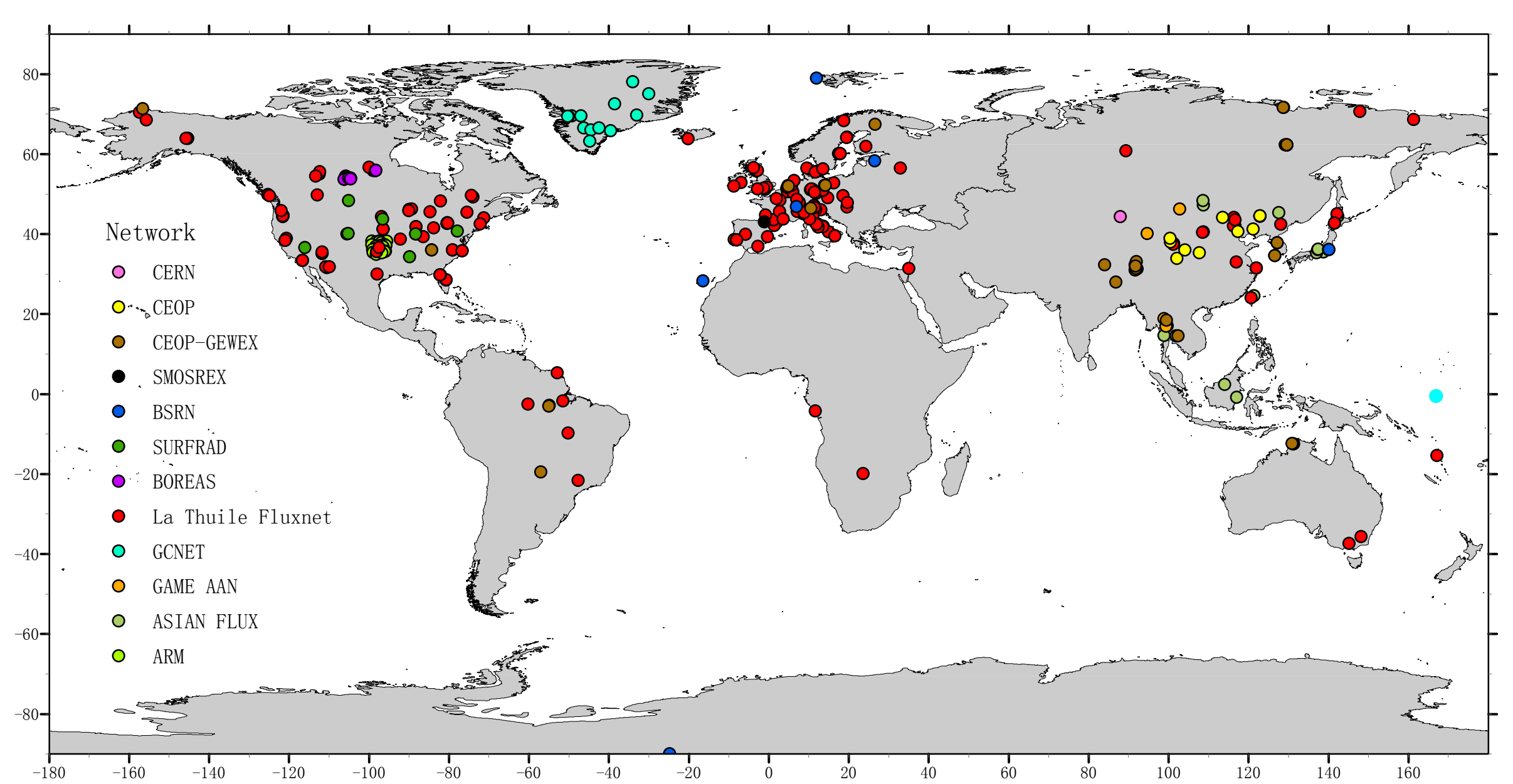
868

869

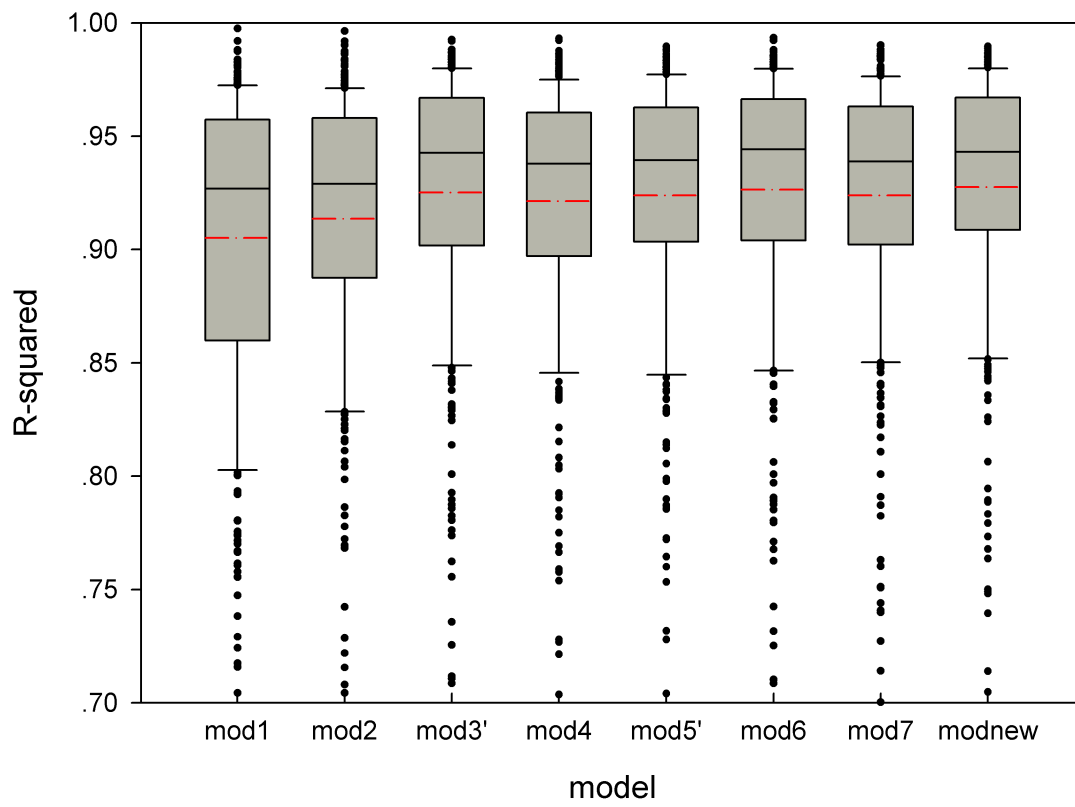
870 Figure 6 Scatter plots showing the differences between the measured and model
871 calculated R_n and related factors for each model in the five categories (S1, S2, S3, S4
872 and global): (a)-(e) daily mean air temperature (T), (f)-(j) daily mean wind speed (W),
873 and (k)-(o) clearness index (CI). Positive values mean that the model underestimated
874 net radiation.

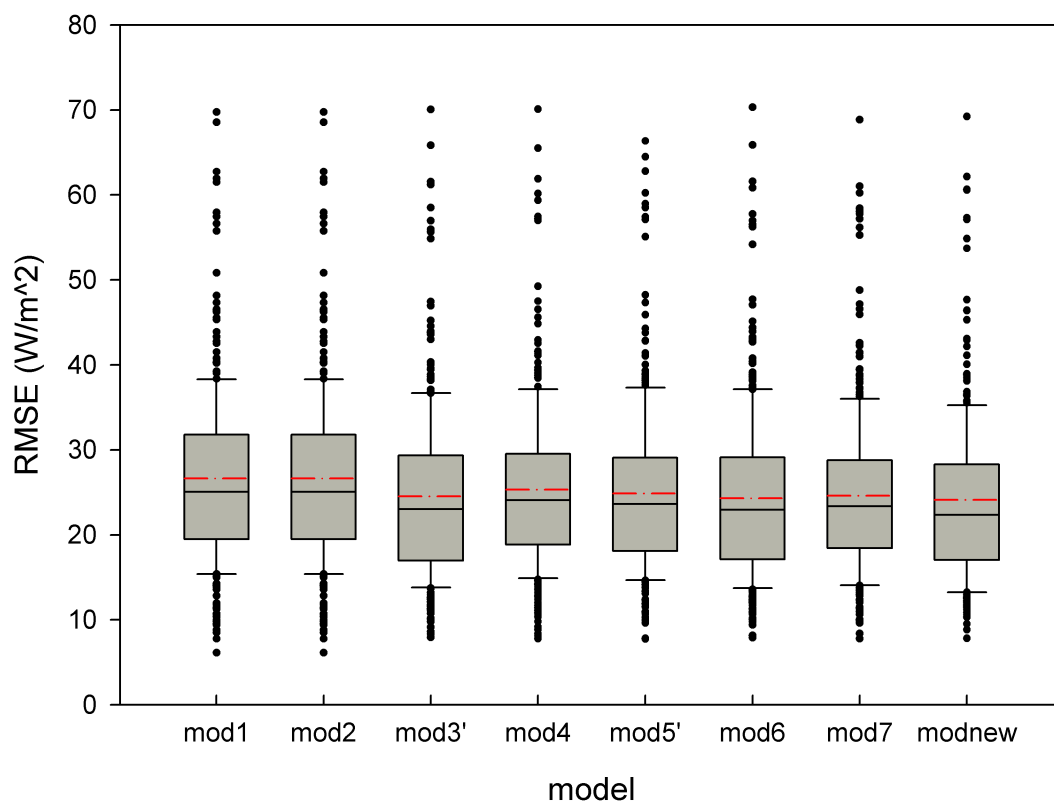
875

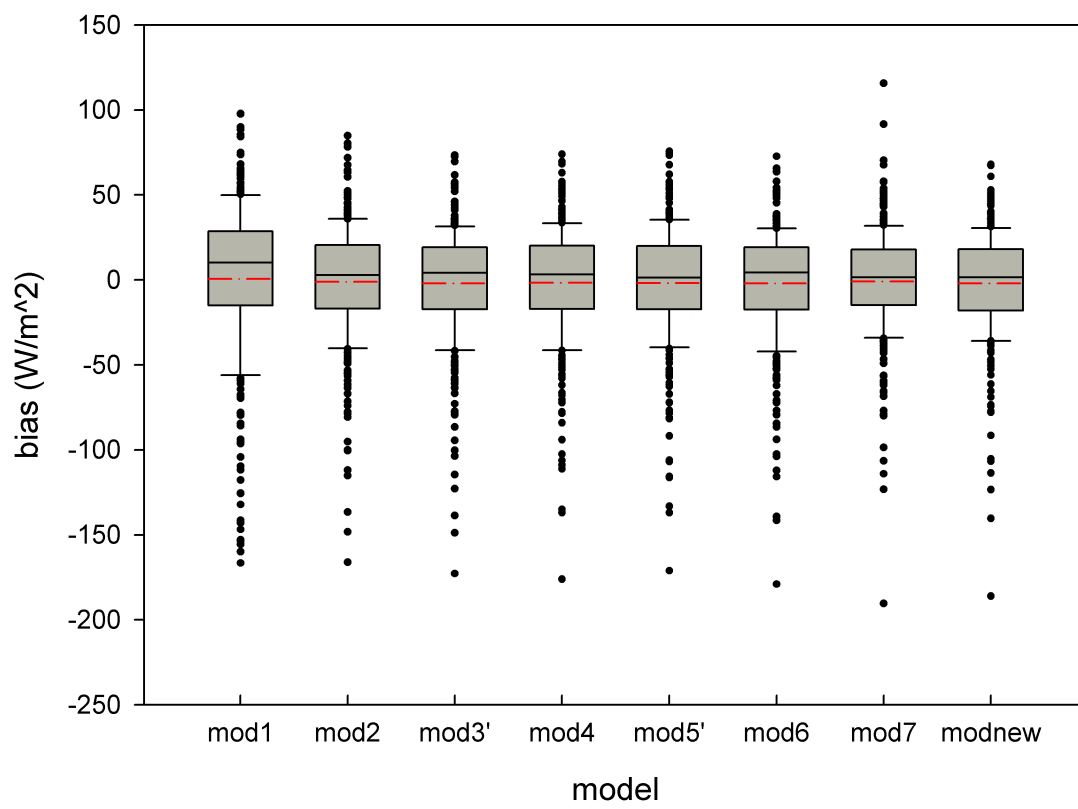
876



2D Graph 5

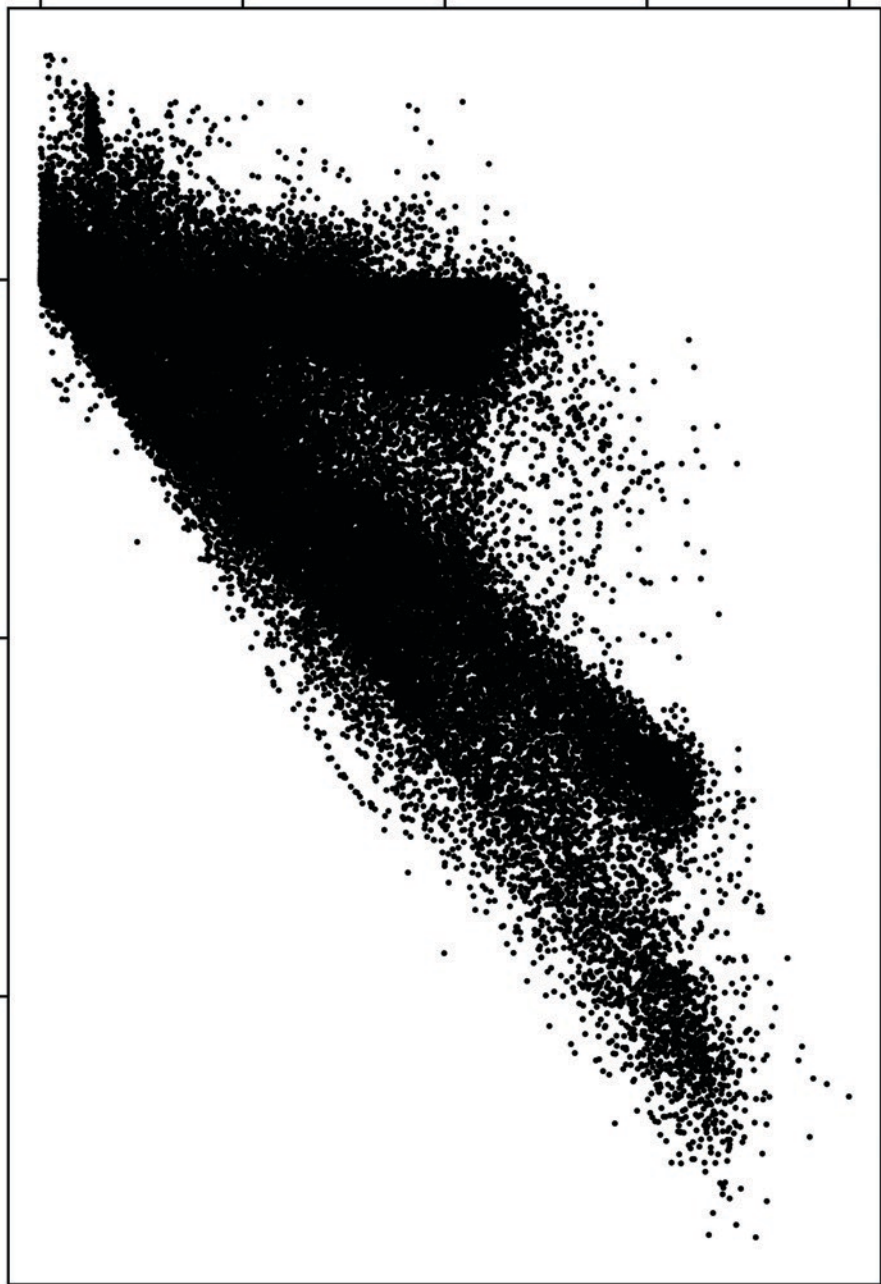






Shortwave radiation Rsi(Wm⁻²)

0 200 400 600 800

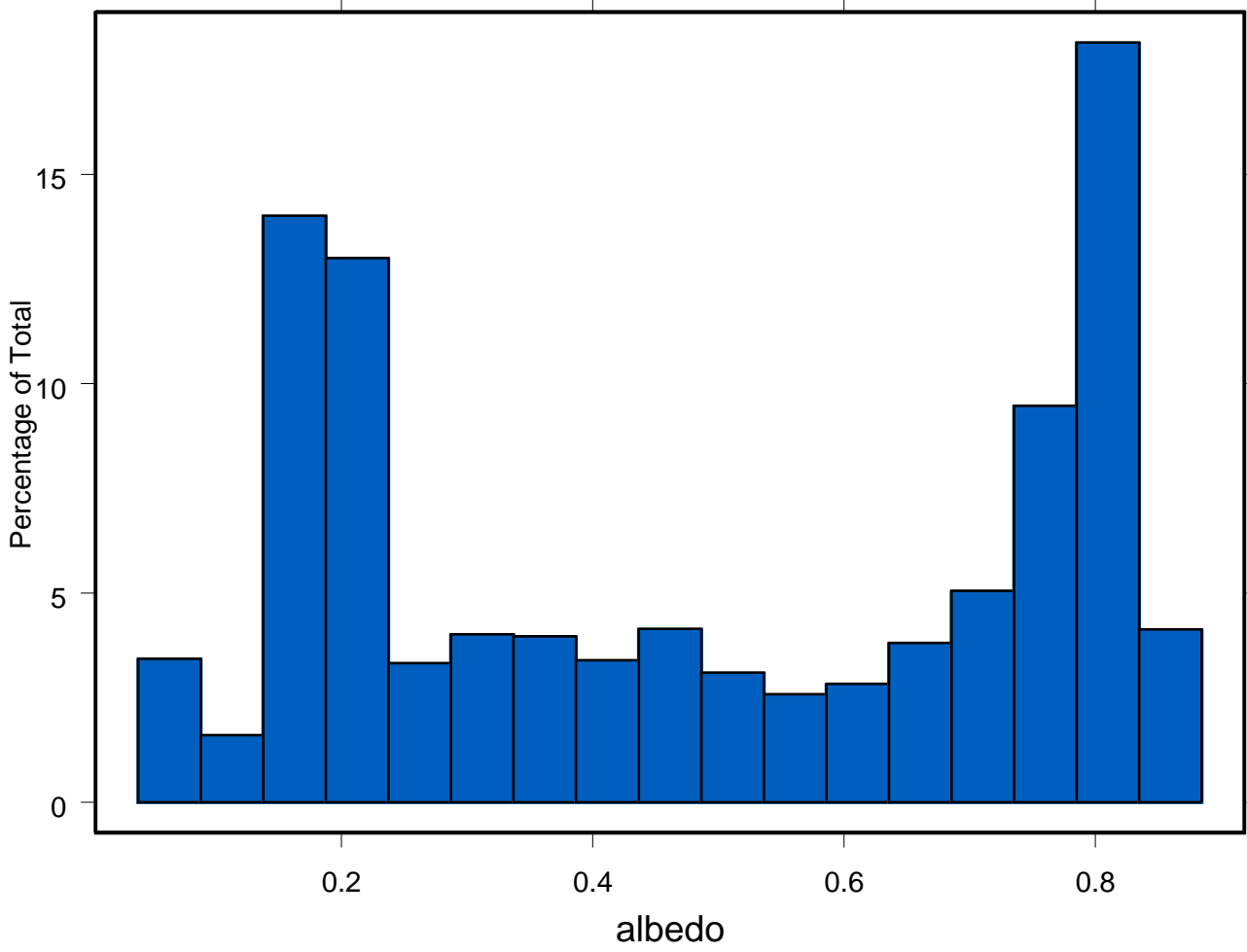


Net radiation Rn (Wm⁻²)

0

200

400



Shortwave radiation Rsi(Wm⁻²)

0 200 400 600 800

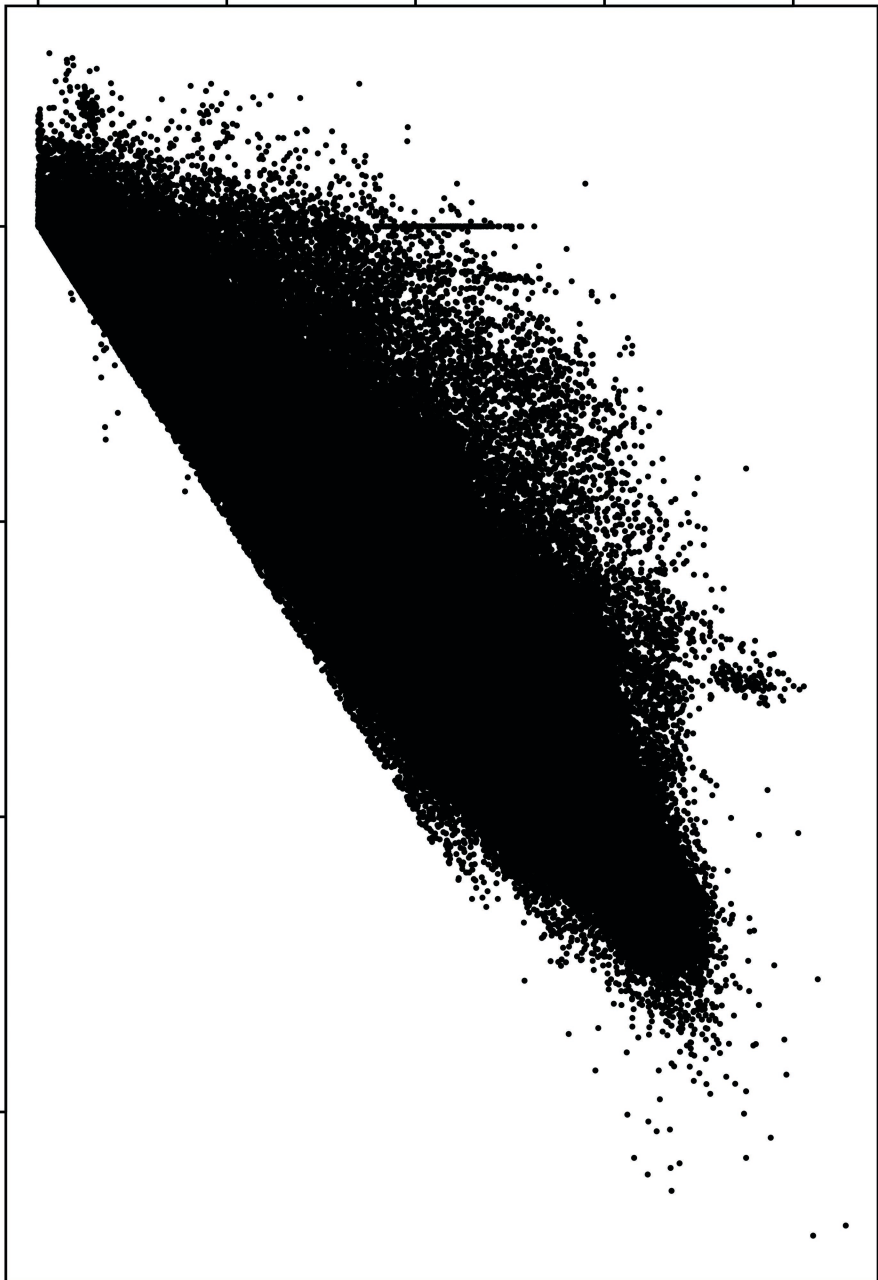
0

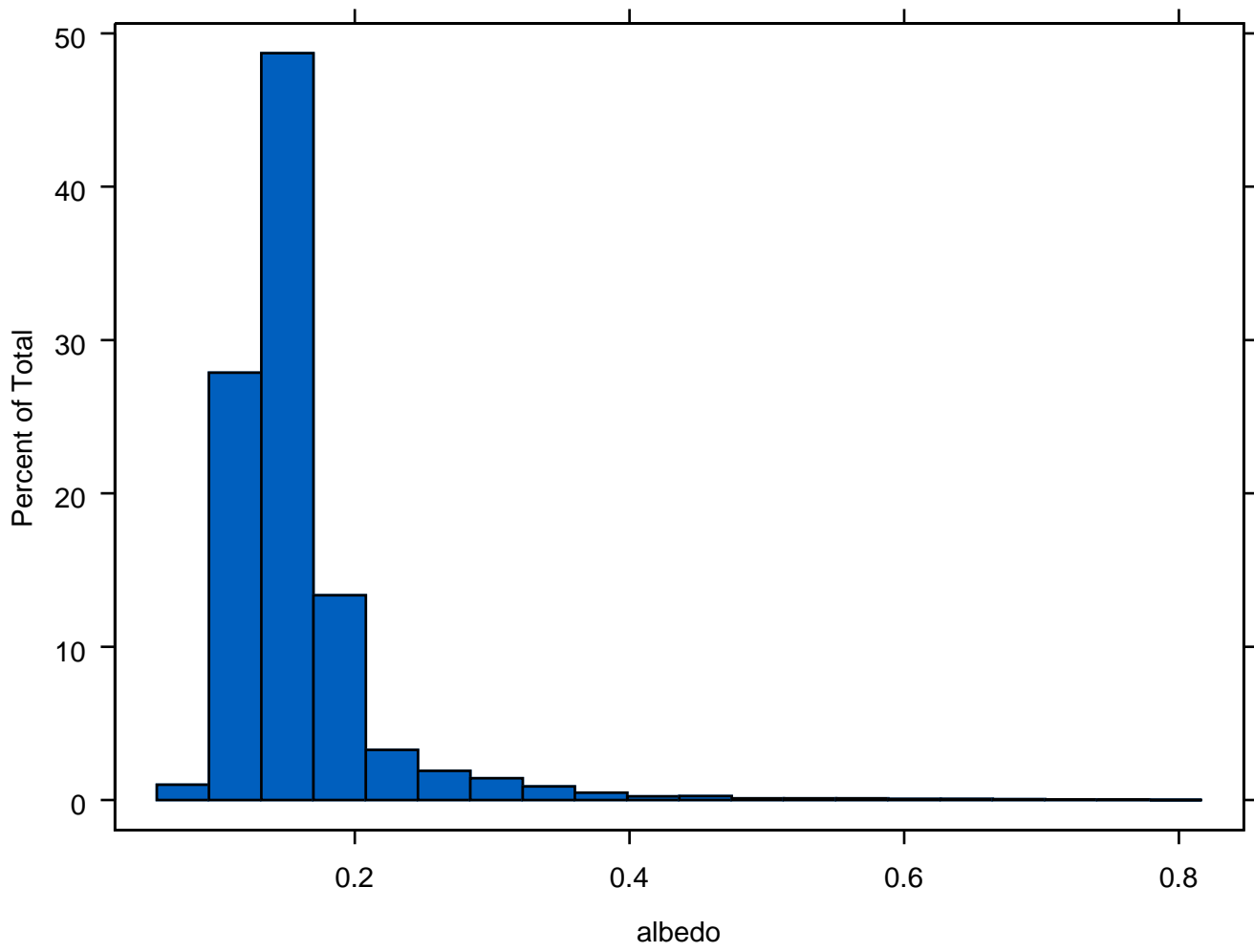
200

400

600

Net radiation Rn (Wm⁻²)





Shortwave radiation Rsi(Wm⁻²)

